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KEY STAGE
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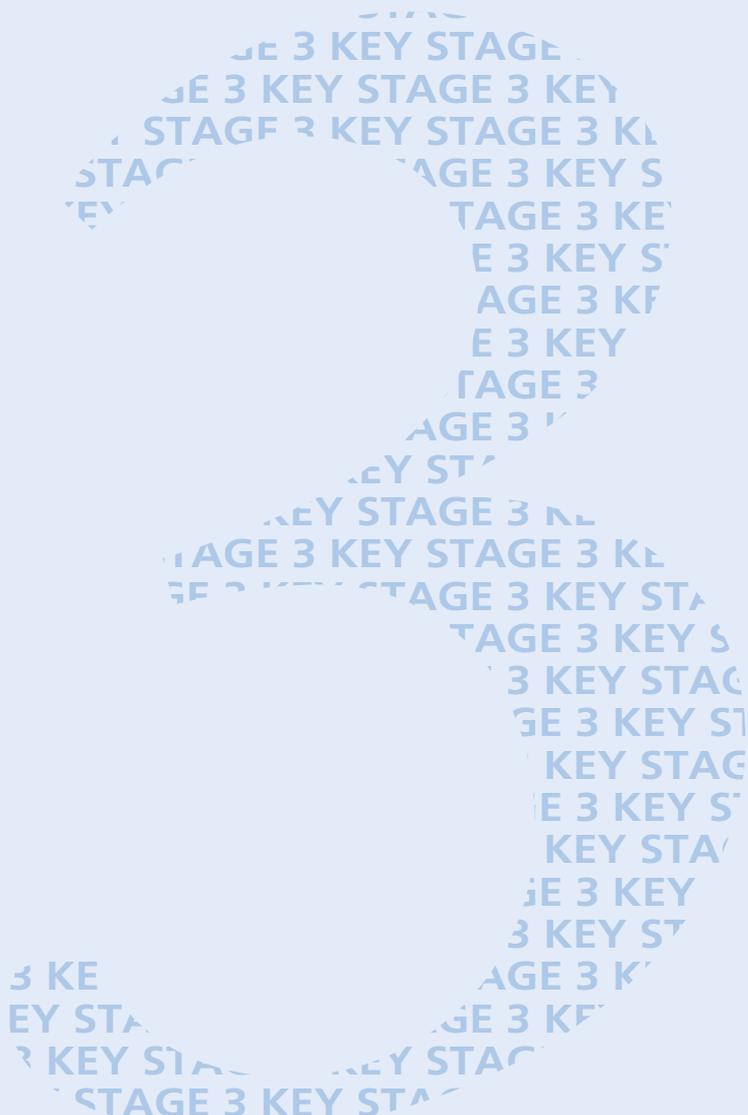
ALL TIERS

2002

Mathematics tests

Mark scheme for Paper 2

Tiers 3–5, 4–6, 5–7 and 6–8



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Guarding standards

Introduction

The test papers will be marked by external markers. The markers will follow the mark scheme in this booklet, which is provided here to inform teachers.

This booklet contains the mark scheme for paper 2 at all tiers. The paper 1 and the extension paper mark schemes are printed in separate booklets. Questions have been given names so that each one has a unique identifier irrespective of tier.

The structure of the mark schemes

The marking information for questions is set out in the form of tables, which start on page 10 of this booklet. The columns on the left-hand side of each table provide a quick reference to the tier, question number, question part, and the total number of marks available for that question part.

The ‘Correct response’ column usually includes two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working, and whether the marks are independent or cumulative;
- examples of some different types of correct response, including the most common and the minimum acceptable.

The ‘Additional guidance’ column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as when ‘follow through’ is allowed, is provided as necessary.

For graphical and diagrammatic responses, including those in which judgements on accuracy are required, marking overlays have been provided as the centre pages of this booklet.

General guidance

Using the mark schemes

Answers that are numerically equivalent or algebraically equivalent are acceptable unless the mark scheme states otherwise.

In order to ensure consistency of marking, the most frequent procedural queries are listed on the following two pages with the prescribed correct action. This is followed by further guidance, relating to marking of questions that involve money, time, coordinates, algebra or probability. Unless otherwise specified in the mark scheme, markers should apply the following guidelines in all cases.

What if ...

<p><i>The pupil's response does not match closely any of the examples given.</i></p>	<p>Markers should use their judgement in deciding whether the response corresponds with the statement of requirements given in the 'Correct response' column. Refer also to the additional guidance.</p>
<p><i>The pupil has responded in a non-standard way.</i></p>	<p>Calculations, formulae and written responses do not have to be set out in any particular format. Pupils may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for indicating a response. Any correct method of setting out working, however idiosyncratic, is acceptable. Provided there is no ambiguity, condone the continental practice of using a comma for a decimal point.</p>
<p><i>The pupil has made a conceptual error.</i></p>	<p>In some questions, a method mark is available provided the pupil has made a computational, rather than conceptual, error. A computational error is a 'slip' such as writing $4 \times 6 = 18$ in an otherwise correct long multiplication. A conceptual error is a more serious misunderstanding of the relevant mathematics; when such an error is seen no method marks may be awarded. Examples of conceptual errors are: misunderstanding of place value, such as multiplying by 2 rather than 20 when calculating 35×27; subtracting the smaller value from the larger in calculations such as $45 - 26$ to give the answer 21; incorrect signs when working with negative numbers.</p>
<p><i>The pupil's accuracy is marginal according to the overlay provided.</i></p>	<p>Overlays can never be 100% accurate. However, provided the answer is within, or touches, the boundaries given, the mark(s) should be awarded.</p>
<p><i>The pupil's answer correctly follows through from earlier incorrect work.</i></p>	<p>'Follow through' marks may be awarded only when specifically stated in the mark scheme, but should not be allowed if the difficulty level of the question has been lowered. Either the correct response or an acceptable 'follow through' response should be marked as correct.</p>
<p><i>There appears to be a misreading affecting the working.</i></p>	<p>This is when the pupil misreads the information given in the question and uses different information. If the original intention or difficulty level of the question is not reduced, deduct one mark only. If the original intention or difficulty level is reduced, do not award any marks for the question part.</p>
<p><i>The correct answer is in the wrong place.</i></p>	<p>Where a pupil has shown understanding of the question, the mark(s) should be given. In particular, where a word or number response is expected, a pupil may meet the requirement by annotating a graph or labelling a diagram elsewhere in the question.</p>

What if ...

<i>The final answer is wrong but the correct answer is shown in the working.</i>	Where appropriate, detailed guidance will be given in the mark scheme, and must be adhered to. If no guidance is given, markers will need to examine each case to decide whether:	
	the incorrect answer is due to a transcription error;	If so, award the mark.
	in questions not testing accuracy, the correct answer has been given but then rounded or truncated;	If so, award the mark.
	the pupil has continued to give redundant extra working which does not contradict work already done;	If so, award the mark.
	the pupil has continued, in the same part of the question, to give redundant extra working which does contradict work already done.	If so, do not award the mark. Where a question part carries more than one mark, only the final mark should be withheld.
<i>The pupil's answer is correct but the wrong working is seen.</i>	A correct response should always be marked as correct unless the mark scheme states otherwise.	
<i>The correct response has been crossed (or rubbed) out and not replaced.</i>	Mark, according to the mark scheme, any legible crossed (or rubbed) out work that has not been replaced.	
<i>More than one answer is given.</i>	If all answers given are correct (or a range of answers is given, all of which are correct), the mark should be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark should be awarded.	
<i>The answer is correct but, in a later part of the question, the pupil has contradicted this response.</i>	A mark given for one part should not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.	

Marking specific types of question

Responses involving money <i>For example: £3.20 £7</i>	
Accept ✓	Do not accept ✗
<ul style="list-style-type: none"> ✓ Any unambiguous indication of the correct amount eg £3.20(p), £3 20, £3,20, 3 pounds 20, £3-20, £3 20 pence, £3:20, £7.00 ✓ The £ sign is usually already printed in the answer space. Where the pupil writes an answer other than in the answer space, or crosses out the £ sign, accept an answer with correct units in pounds and/or pence eg 320p, 700p 	<ul style="list-style-type: none"> ✗ Incorrect or ambiguous use of pounds or pence eg £320, £320p or £700p, or 3.20 or 3.20p not in the answer space. ✗ Incorrect placement of decimal points, spaces, etc or incorrect use or omission of 0 eg £3.2, £3 200, £32 0, £3-2-0, £7.0

Responses involving time <i>A time interval For example: 2 hours 30 mins</i>	
Accept ✓	Take care ! Do not accept ✗
<ul style="list-style-type: none"> ✓ Any unambiguous indication eg 2.5 (hours), 2h 30 ✓ Digital electronic time ie 2:30 	<ul style="list-style-type: none"> ✗ Incorrect or ambiguous time interval eg 2.3(h), 2.30, 2-30, 2h 3, 2.30min ! The time unit, hours or minutes, is usually printed in the answer space. Where the pupil writes an answer other than in the answer space, or crosses out the given unit, accept an answer with correct units in hours or minutes, unless the question has asked for a specific unit to be used.
A specific time For example: 8.40am, 17:20	
Accept ✓	Do not accept ✗
<ul style="list-style-type: none"> ✓ Any unambiguous, correct indication eg 08.40, 8.40, 8:40, 0840, 8 40, 8-40, twenty to nine, 8,40 ✓ Unambiguous change to 12 or 24 hour clock eg 17:20 as 5:20pm, 17:20pm 	<ul style="list-style-type: none"> ✗ Incorrect time eg 8.4am, 8.40pm ✗ Incorrect placement of separators, spaces, etc or incorrect use or omission of 0 eg 840, 8:4:0, 084, 84

Responses involving coordinates For example: (5, 7)	
Accept ✓	Do not accept ✗
✓ Unambiguous but unconventional notation eg (05, 07) (five, seven) $\begin{matrix} x & y \\ (5, & 7) \end{matrix}$ $(x = 5, y = 7)$	✗ Incorrect or ambiguous notation eg (7, 5) $(5x, 7y)$ $(x5, y7)$ $(5^x, 7^y)$

Responses involving the use of algebra For example: $2 + n$ $n + 2$ $2n$	
Accept ✓	Take care ! Do not accept ✗
✓ The unambiguous use of a different case eg N used for n ✓ Unconventional notation for multiplication eg $n \times 2$ or $2 \times n$ or $n2$ or $n + n$ for $2n$ $n \times n$ for n^2 ✓ Multiplication by 1 or 0 eg $2 + 1n$ for $2 + n$ $2 + 0n$ for 2 ✓ Words used to precede or follow equations or expressions eg $t = n + 2$ tiles or tiles = $t = n + 2$ for $t = n + 2$ ✓ Unambiguous letters used to indicate expressions eg $t = n + 2$ for $n + 2$ ✓ Embedded values given when solving equations eg $3 \times 10 + 2 = 32$ for $3x + 2 = 32$! Words or units used within equations or expressions should be ignored if accompanied by an acceptable response, but should not be accepted on their own eg do not accept n tiles + 2 n cm + 2 ✗ Change of variable eg x used for n ✗ Ambiguous letters used to indicate expressions eg $n = n + 2$ However, to avoid penalising any of the three types of error above more than once within each question, do not award the mark for the <i>first</i> occurrence of each type within each question. Where a question part carries more than one mark, only the final mark should be withheld. ✗ Embedded values that are then contradicted eg for $3x + 2 = 32$, $3 \times 10 + 2 = 32, x = 5$

Responses involving probability A numerical probability should be expressed as a decimal, fraction or percentage only. <i>For example: 0.7</i>	
Accept ✓	Take care ! Do not accept ✗
<ul style="list-style-type: none"> ✓ A correct probability that is correctly expressed as a decimal, fraction or percentage. ✓ Equivalent decimals, fractions or percentages eg 0.700, $\frac{70}{100}$, $\frac{35}{50}$, 70.0% ✓ A probability correctly expressed in one acceptable form which is then incorrectly converted, but is still less than 1 and greater than 0 eg $\frac{70}{100} = \frac{18}{25}$ 	<p>The following four categories of error should be ignored if accompanied by an acceptable response, but should not be accepted on their own.</p> <ul style="list-style-type: none"> ! A probability that is incorrectly expressed eg 7 in 10, 7 out of 10, 7 from 10 ! A probability expressed as a percentage without a percentage sign. ! A fraction with other than integers in the numerator and/or denominator. However, each of the three types of error above should not be penalised more than once within each question. Do not award the mark for the <i>first</i> occurrence of each type of error unaccompanied by an acceptable response. Where a question part carries more than one mark, only the final mark should be withheld. ! A probability expressed as a ratio eg 7 : 10, 7 : 3, 7 to 10 ✗ A probability greater than 1 or less than 0

Recording marks awarded on the test paper

All questions, even those not attempted by the pupil, will be marked, with a 1 or a 0 entered in each marking space. Where 2m can be split into 1m gained and 1m lost, with no explicit order, then this will be recorded by the marker as 1
0

The total marks awarded for a double page will be written in the box at the bottom of the right-hand page, and the total number of marks obtained on the paper will be recorded on the front of the test paper.

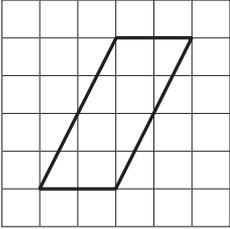
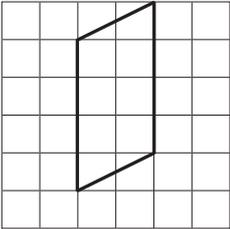
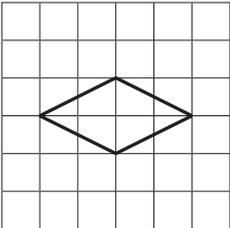
A total of 120 marks is available in each of tiers 3–5, 4–6, 5–7 and 6–8. The extension paper carries 42 marks.

Awarding levels

The sum of the marks gained on paper 1, paper 2 and the mental arithmetic paper determines the level awarded. Level threshold tables, which show the mark ranges for the award of different levels, will be available on the QCA website (www.qca.org.uk) from Wednesday 26 June 2002. QCA will also send a copy to each school in July.

Schools will be notified of pupils' results by means of a marksheet, which will be returned to schools by the External Marking Agency with the pupils' marked scripts. The marksheet will include pupils' scores on the test papers and the levels awarded.

Tier & Question					Holiday	
3-5	4-6	5-7	6-8			
3					Correct response	Additional guidance
a				1m	£ 10	<p>✗ <i>Incorrect response</i></p> <p>eg</p> <p>♦ - 10</p>
b				3m <i>or</i> 2m	<p>£ 22</p> <p>Shows the digits 22</p> <p>eg</p> <ul style="list-style-type: none"> ■ 220 ■ 2.20 <p>or</p> <p>Shows the values 586 and 608</p> <p>or</p> <p>Shows one of the values 586 and 608 and correctly subtracts using their incorrect total</p> <p>eg</p> <ul style="list-style-type: none"> ■ Woman 586, man 648 (<i>error</i>), 648 - 586 = 62 ■ 194 + 196 + 196 = 486 (<i>error</i>) 289 + 319 = 608 so it's 122 more <p>or</p> <p>Shows a complete correct method with the only error in the final answer</p> <p>eg</p> <ul style="list-style-type: none"> ■ 289 + 319 - (194 + 196 + 196) = 32 (<i>error</i>) 	
				<i>or</i> 1m	Shows one of the values 586 or 608	

Tier & Question						Correct response	Additional guidance
3-5	4-6	5-7	6-8	4			
a					1m	Draws a square	<p>! <i>Lines not ruled, or internal lines drawn</i> Accept provided the pupil's intention is clear</p>
b					1m	Draws a rectangle, or draws a square that is a different size from the one in part (a)	
c					1m	Draws a parallelogram with no right angles eg ■  ■  ■ 	
d					2m All four entries correct, ie 4 4 2 4 or 1m At least two entries correct	<p>✓ <i>Unambiguous indication that the sides are the same length</i> eg, for the final value of 4</p> <ul style="list-style-type: none"> ◆ All ◆ The ◆ Yes 	

Tier & Question					School trip	
3-5	4-6	5-7	6-8			
5					Correct response	Additional guidance
a				1m	60	
b				2m <i>or</i> 1m	All three correct, ie 5 6 10 Any two correct	

Tier & Question					Place names	
3-5	4-6	5-7	6-8			
6	1				Correct response	Additional guidance
a	a			1m	49	
b	b			1m	30	

Tier & Question										Dinner time		
3-5	4-6	5-7	6-8									
7	2			Correct response				Additional guidance				
a	a			2m	All three rows correct, ie <div style="display: flex; justify-content: space-around; margin-bottom: 5px;"> <input type="checkbox"/> <input type="checkbox"/> <input checked="" type="checkbox"/> </div> <div style="display: flex; justify-content: space-around; margin-bottom: 5px;"> <input type="checkbox"/> <input type="checkbox"/> <input checked="" type="checkbox"/> </div> <div style="display: flex; justify-content: space-around;"> <input checked="" type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> </div>				! <i>Frequencies shown</i> For 2m or 1m, if the correct box for a row has been identified ignore any frequencies shown, even if incorrect. If the correct box for a row has not been identified, and all 9 frequencies are correct, mark as 1, 0 eg <ul style="list-style-type: none"> • <input type="checkbox"/>38 <input type="checkbox"/>18 <input type="checkbox"/>42 <input type="checkbox"/>36 <input type="checkbox"/>26 <input type="checkbox"/>44 <input type="checkbox"/>36 <input type="checkbox"/>28 <input type="checkbox"/>30 			
				or 1m	Any two rows correct							
b	b			2m	12							
				or 1m	Shows at least one of the following totals: 106 (or 70), 94 (or 58) or Shows both of the differences 2 and 14, with no evidence of an incorrect method							
									! <i>Signs incorrect</i> Ignore			

Tier & Question						Which calculation?	
3-5	4-6	5-7	6-8				
8	3			Correct response		Additional guidance	
a	a			1m	Joins the first to $4 - 3$	The following shows the correct responses: 	
				1m	Joins the second to $(3 \times 27) + (4 \times 25)$		
				1m	Joins the third to $(4 \times 25) - (3 \times 27)$		
b	b			1m	<p>The question refers to the total number of pupils in year 9 eg</p> <ul style="list-style-type: none"> ■ Altogether, how many people are in year 9? ■ How many pupils are there in year 9? <p>or</p> <p>The question refers to both 4 and 25, and interprets the significance of the multiplication sign eg</p> <ul style="list-style-type: none"> ■ How many pupils are there altogether in 4 classes of 25? <p>or</p> <p>Interprets the calculation in a valid way whilst still referring to year 9 eg</p> <ul style="list-style-type: none"> ■ If there were always 4 classes in year 9, how many classes would there have been in 25 years? 	<p>✓ <i>Response is a statement rather than a question</i> eg, for the first category</p> <ul style="list-style-type: none"> ♦ It's the total number of people in year 9 ♦ All the pupils in all the classes in the oldest year <p>✗ <i>Incomplete response</i> eg</p> <ul style="list-style-type: none"> ♦ How many pupils altogether? <p>✓ <i>Response processes the 4×25 correctly</i> eg</p> <ul style="list-style-type: none"> ♦ Altogether there are 100 pupils in year 9 ♦ 100 pupils are in year 9 <p>✗ <i>Incomplete response</i> eg</p> <ul style="list-style-type: none"> ♦ How many pupils altogether in 4 classes? ♦ It's the number of classes in year 9 with the number of students ♦ Four classes with 25 pupils in year 9 <p>✗ <i>Response does not refer to the given context</i> eg</p> <ul style="list-style-type: none"> ♦ 25 pupils each have 4 rulers. How many rulers do they have altogether? <p>✗ <i>Response matches a different calculation</i> eg</p> <ul style="list-style-type: none"> ♦ If there are 100 students in year 9 and only 4 teachers, how many pupils are in each class? 	

Tier & Question									Throwing coins	
3-5	4-6	5-7	6-8							
9	4					Correct response		Additional guidance		
a	a				1m	<p>Indicates 'True' and gives a correct explanation that implies there are two outcomes, both of which are equally likely</p> <p>eg</p> <ul style="list-style-type: none"> ■ There are two equally likely possibilities, heads or tails ■ A head is just as likely as a tail ■ Both sides are equally likely 	<p>✓ <i>Minimally acceptable explanation</i></p> <p>eg, implicit reference to equally likely</p> <ul style="list-style-type: none"> ♦ There are 2 sides ♦ It can land on H or T <p>eg, implicit reference to two outcomes</p> <ul style="list-style-type: none"> ♦ It's 50 – 50 ♦ It's an even chance ♦ As it's a fair coin <p>✗ <i>Incomplete explanation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ You don't know what will come up next ♦ Coins sometimes land on heads ♦ It is equal ♦ It's a fair chance 			
b	b				1m	<p>Indicates 'False' and gives a correct explanation</p> <p>The most common correct explanations:</p> <p>State the outcome cannot be predicted with certainty</p> <p>eg</p> <ul style="list-style-type: none"> ■ Each throw is random ■ You don't know what you will get. It's just chance ■ You don't know until you've thrown ■ You never know which side the coin will land on <p>Show there are alternative outcomes</p> <p>eg</p> <ul style="list-style-type: none"> ■ You might get 4 heads ■ There are more possibilities like HHHH, HHHT, HHTH and so on ■ You could get just one tail 	<p>✓ <i>Minimally acceptable explanation</i></p> <p>eg, for the first category</p> <ul style="list-style-type: none"> ♦ It's random ♦ It's chance <p>eg, for the second category</p> <ul style="list-style-type: none"> ♦ You might get something different ♦ You don't know that's what you'll get ♦ Each one could land on any side <p>! <i>Explanation refers to one throw of one coin</i></p> <p>Condone provided reference is made to both uncertainty and two outcomes</p> <p>eg</p> <ul style="list-style-type: none"> ♦ It can land on either side ♦ It could land on H or T <p>✗ <i>Incomplete explanation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ It could be anything ♦ You don't know ♦ It's not certain <p>✗ <i>Incorrect or ambiguous explanation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ There are five different outcomes ♦ You are as likely to get 3 heads and 1 tail ♦ It's 50 – 50 			

Tier & Question									Folding	
3-5	4-6	5-7	6-8							
10	5					Correct response		Additional guidance		
a	a			2m	Both correct, ie 12 by 4 (either order) and 6 by 8 (either order)					
				or 1m	One correct, the other incorrect or omitted					
b	b			1m	3					

Tier & Question									Yards	
3-5	4-6	5-7	6-8							
11	6	1				Correct response		Additional guidance		
a	a	a		1m	91.44			✓ 91 or 91.4		
b	b	b		2m	109 or 109(...) with no evidence of an incorrect method			<p>! <i>Answer of 110</i> Accept provided a more accurate value or a correct method is seen</p> <p>✗ <i>Correct answer from an incorrect method</i> eg ♦ $100 - 91.44 = 8.56$, $100 + 8.56$ is about 109</p> <p>! <i>Answers to parts (a) and (b) reversed</i> Treat as a misread and deduct the first mark only</p>		
				or 1m	Shows the digits 109(...) but the decimal point is positioned incorrectly or omitted					
					or					
					Shows the correct inverse operations, in any order eg ■ $\times 100, \div 2.54, \div 36$					
					or					
					Shows $\div 91.44$					

Tier & Question									Scales		
3-5	4-6	5-7	6-8								
12	7	2			Correct response		Additional guidance				
a	a				1m	14 to 14.2 inclusive					
b	b				1m	220 to 230 inclusive		✓ <i>Fractional value</i>			
c	c				2m	35 to 36 inclusive		<p>! <i>Follow through from part (a)</i> Accept provided it is explicit in the working that the method incorporates this incorrect value</p> <p>✗ <i>Poor mathematical communication</i> Do not infer incorrect reading of the scale eg</p> <ul style="list-style-type: none"> • 3×10 (No indication of method through written working or through markings on the scale, and answer to the calculation is outside the acceptable range) 			
					or 1m	<p>Shows how to use the scale to find 1000g, even if the scale is read incorrectly eg</p> <ul style="list-style-type: none"> ■ Work out what it is for 100g, then $\times 10$ ■ $400\text{g} + 400\text{g} + 200\text{g}$ ■ 200g is 7, 5×7 ■ 100g is 4 (<i>error</i>) ounces, 4×10 ■ 500g is 17 (<i>error</i>), then double 17 ■ 250 is 9, $9 \times 4 = 32$ (<i>error</i>) <p>or</p> <p>Shows a correct multiplication, or a correct addition, that would give an answer within the correct range, even if this is followed by incorrect processing eg</p> <ul style="list-style-type: none"> ■ 3.6×10 ■ 5×7 ■ $14 + 14 + 7$ 					

Tier & Question					Security lock	
3-5	4-6	5-7	6-8			
13	8	3			Correct response	Additional guidance
a	a	a		2m <i>or</i> 1m	<p>24, with no incorrect working</p> <p>Shows a correct method eg</p> <ul style="list-style-type: none"> ■ 4×6 ■ There are 6 ways for the letter A and it is the same for each of the other letters <p>or</p> <p>Lists in a systematic way for any one of the letters or any one of the numbers eg</p> <ul style="list-style-type: none"> ■ C1, C2, C3, C4, C5, C6 ■ A / 6, 5, 4, 3, 2, 1 ■ A1, B1, C1, D1 	<p>× 24 obtained from listing that includes duplication</p>
b	b	b		1m	$\frac{1}{6}$ or equivalent probability	<p>! <i>Decimal or percentage rounded or truncated</i> Accept 0.17 or 0.167 or 0.166(...), or the equivalent % values. Do not accept 0.16</p>

Tier & Question					Screenwash	
3-5	4-6	5-7	6-8			
14	9	4			Correct response	Additional guidance
a	a	a		1m	600	
b	b	b		1m	50	
b	b	b		1m	<p>Indicates 'No' and gives a correct explanation</p> <p>The most common correct explanations:</p> <p>State that 25% implies a total of 4 parts but there are 5 eg</p> <ul style="list-style-type: none"> ■ There are 5 parts not 4 ■ There are 4 parts of water not 3 <p>State what 25% would imply eg</p> <ul style="list-style-type: none"> ■ 25% would be 1 part screenwash to 3 parts water ■ It would give a total of 125% <p>Refer to the correct percentage of 20% eg</p> <ul style="list-style-type: none"> ■ It's 20% ■ 1 out of 5 = 20 out of 100 	<p>✓ <i>Minimally acceptable explanation</i> eg, for the first category</p> <ul style="list-style-type: none"> ♦ 1 : 4 means 5 parts altogether ♦ It's 1 out of 5 ♦ There are 5 parts <p>✓ <i>Use of information from part (a)</i> eg</p> <ul style="list-style-type: none"> ♦ $150\text{ml} \times 5 = 750$ not 600 <p>× <i>Incomplete explanation</i> eg</p> <ul style="list-style-type: none"> ♦ It's less than a quarter screenwash ♦ It's more than 75% water ♦ There are more than 4 parts ♦ 1 part with 4 parts

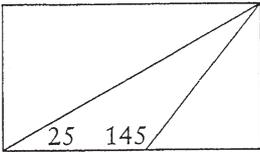
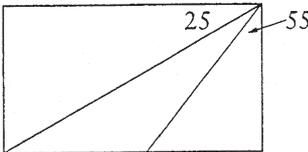
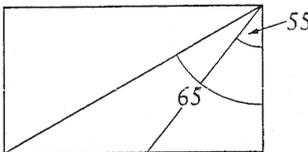
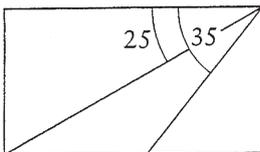
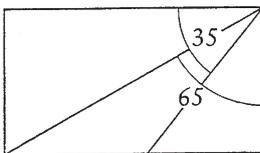
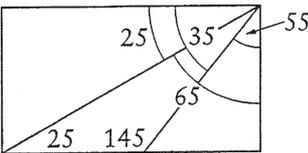
Tier & Question				Marking overlay available		Net
3-5	4-6	5-7	6-8			
15	10	5		Correct response		Additional guidance
a	a	a		1m	<p>Indicates the correct shape, ie</p> 	
b	b	b		1m	<p>Lines correct ie uses a ruler to draw both straight lines from a common point, within the tolerance for length as implied by the overlay</p>	<p>✓ <i>Lines correct length but outside of the arcs shown on the overlay</i></p>
				1m	<p>Angle correct ie draws or indicates the angle within the tolerance as shown on the overlay</p>	
				1m	<p>Arc correct ie draws the arc within the tolerance as shown on the overlay. (Ignore continuation of the arc beyond the lines denoting the angle)</p>	
<p>✓ <i>Follow through from an incorrect angle</i></p> <p>! <i>Follow through from incorrect straight lines</i> Accept, provided both lines are the same length and compasses have been used. Note the dashed lines on the overlay are a visual aid to help identify those who have not used compasses</p> <p>✗ <i>Arc shown as a series of points</i></p> <p>! <i>Extra information added to the net in an attempt to show a 3-D drawing</i> Penalise one mark only, by withholding the final mark that would otherwise have been awarded</p>						

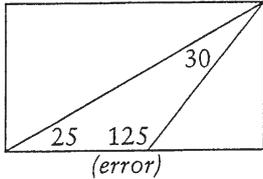
Tier & Question						Piles of cards	
3-5	4-6	5-7	6-8				
16	11	6			Correct response	Additional guidance	
a	a	a		1m	Correct expression eg <ul style="list-style-type: none"> ■ $4n + 5$ ■ $6n + 8 - (2n + 3)$ 	✗ Incorrect expression eg, for part (a) <ul style="list-style-type: none"> ♦ $6n + 8 - 2n + 3$ eg, for part (b) <ul style="list-style-type: none"> ♦ $6n + 8 \div 2$ 	
b	b	b		1m	Correct expression eg <ul style="list-style-type: none"> ■ $3n + 4$ ■ $\frac{6n + 8}{2}$ ■ $(6n + 8) \div 2$ 	✓ Correct expression repeated eg <ul style="list-style-type: none"> ♦ $3n + 4$ and $3n + 4$ 	
c	c	c		2m	105		
				or 1m	Shows the value 20 or Using an incorrect value of n , evaluates $5n + 5$ correctly eg, from $n = 26$ <ul style="list-style-type: none"> ■ $5 \times 26 + 5 = 135$ eg, from $n = 23$ <ul style="list-style-type: none"> ■ 120 or Using an incorrect value of n , evaluates $6n + 8$ correctly and then subtracts 23 eg, from $n = 24$ <ul style="list-style-type: none"> ■ $6 \times 24 + 8 = 152, 152 - 23 = 129$ eg, from $n = 23$ <ul style="list-style-type: none"> ■ $6 \times 23 + 8 = 146, 146 - 23 = 123$! Value for n if not stated Accept if embedded eg <ul style="list-style-type: none"> ♦ $5 \times 21 + 5 = 110$ Do not accept if not specified and not embedded eg <ul style="list-style-type: none"> ♦ 120 (neither $n = 23$, nor $5 \times 23 + 5$ shown) 	

Cycling

Tier & Question					Correct response	Additional guidance
3-5	4-6	5-7	6-8			
17	12	7				
				2m	<p>Gives a correct explanation</p> <p>The most common correct explanations:</p> <p>Show the mean is 39.9 which is less than 40 eg</p> <ul style="list-style-type: none"> ■ $32.3 + 38.7 + 43.5 + 45.1 = 159.6$, $159.6 \div 4 = 39.9$ which is 0.1 too small ■ $39.9 < 40$ <p>Show the total distance is 159.6 which is less than 160 eg</p> <ul style="list-style-type: none"> ■ $40 \times 4 = 160$, $160 > 159.6$ <p>Compare and interpret the daily differences in distance from 40 eg</p> <ul style="list-style-type: none"> ■ $-7.7 + -1.3 + 3.5 + 5.1 = -0.4$ so it's under 40 ■ $7.7 + 1.3 > 3.5 + 5.1$ 	<p>! <i>Response does not refer to 40</i> eg</p> <ul style="list-style-type: none"> • The mean is 39.9 <p>Accept provided this is not accompanied by an incorrect statement eg, for 2m do not accept</p> <ul style="list-style-type: none"> • $159.6 \div 4 = 39.9$ so she rode more than 40km a day <p>! <i>That 159.6 is less than 160 is not stated explicitly</i> The values of 159.6 and 160 must be shown, but accept implicit comparison eg</p> <ul style="list-style-type: none"> • It's 159.6 not 160 <p>As in the previous category, for 2m do not accept a correct response accompanied by an incorrect statement</p> <p>× <i>No interpretation</i> eg</p> <ul style="list-style-type: none"> • On Mon she did 7.7km less, Tues was 1.3km less, Wed was 3.5km more, Thurs was 5.1km more <p>! <i>Values rounded</i> eg</p> <ul style="list-style-type: none"> • $32 + 39 + 44 + 45 = 160$ so the mean is 40 <p>Mark as 1, 0</p> <p>! <i>Median calculated correctly</i> Accept for 1m, provided the word median is used and the statement is contradicted eg, accept for 1m</p> <ul style="list-style-type: none"> • The median is 41.1 so she is correct <p>eg, do not accept</p> <ul style="list-style-type: none"> • The average is 41.1 so she is correct <p>× <i>Incomplete method with no evaluation or interpretation</i> eg</p> <ul style="list-style-type: none"> • $(32.3 + 38.7 + 43.5 + 45.1) \div 4$
				or 1m	<p>Shows the value 159.6 or 160</p> <p>or</p> <p>Shows a correct method to find the mean, or the difference between the mean and 40, with not more than one computational error eg</p> <ul style="list-style-type: none"> ■ $32.3 + 38.7 + 43.5 + 45.1 = 158.6$ (error) $158.6 \div 4 = 39.65$ ■ -8.7 (error) $-1.3 + 3.5 + 5.1 = -1.4$ <p>or</p> <p>Describes a complete correct method but does not completely evaluate eg</p> <ul style="list-style-type: none"> ■ When you add them all up it doesn't come to more than 4×40 	

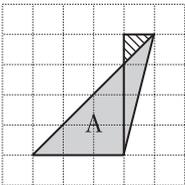
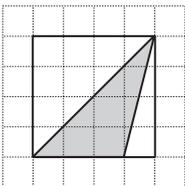
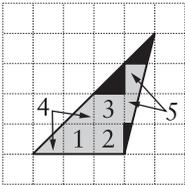
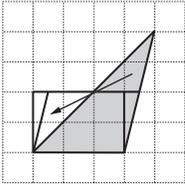
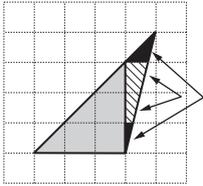
Tier & Question						Same volume	
3-5	4-6	5-7	6-8				
	13	8	1			Correct response	Additional guidance
	a	a	a	1m	Correct volume, ie 60	<p>! <i>The value of 60 is shown to the power of 3</i></p> <p>eg</p> <ul style="list-style-type: none"> • 60^3 • 60^3cm <p>Assume the power refers to units, ie mark as 1, 0</p> <p>✓ <i>Informal but unambiguous language</i></p> <p>eg</p> <ul style="list-style-type: none"> • Cube centimetres 	
				1m	<p>Correct units</p> <p>eg</p> <ul style="list-style-type: none"> ■ cm^3 ■ Centimetres cubed 		
	b	b	b	1m	6	<p>! <i>Follow through as their part (a) $\div 10$</i></p> <p>Accept provided the value is exact and not rounded</p> <p>! <i>Incorrect units inserted</i></p> <p>Ignore</p>	

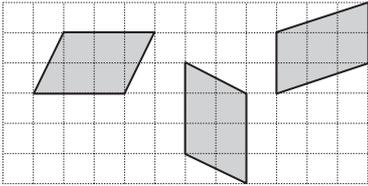
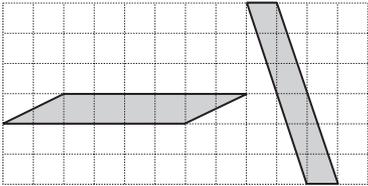
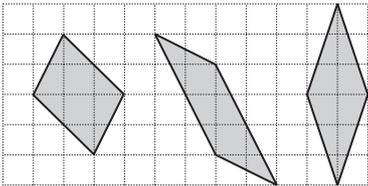
Tier & Question					Correct response	Additional guidance
3-5	4-6	5-7	6-8			
14	9	2				Angles again
				3m	<p>10, with a correct and unambiguous method that clearly identifies the relevant angles being used by use of letters or, minimally, on the diagram</p> <p>The most common correct methods:</p> <p>Calculate $\angle CAK$ and $\angle AKC$ eg</p> <ul style="list-style-type: none"> ■ $\angle CAK = 25$ ($90 - 65$) ■ $\angle AKC = 145$ ($180 - 35$) ■ $180 - 25 - 145$ <p>Use triangles ADC and KCB eg</p> <ul style="list-style-type: none"> ■ $\angle ACD = 25$ ($180 - 90 - 65$) ■ $\angle KCB = 55$ ($180 - 90 - 35$) ■ $90 - 25 - 55$ <p>Use alternate angles to find $\angle ACB$ then subtract $\angle KCB$ eg</p> <ul style="list-style-type: none"> ■ $\angle ACB = 65$ (alternate angles) ■ $\angle KCB = 55$ ($180 - 90 - 35$) ■ $65 - 55$ <p>Use alternate angles to find $\angle KCD$ then subtract $\angle ACD$ eg</p> <ul style="list-style-type: none"> ■ $\angle KCD = 35$ (alternate angles) ■ $\angle ACD = 25$ ($90 - 65$) ■ $35 - 25$ <p>Use alternate angles to find $\angle ACB$ and $\angle KCD$, and recognise that the total of these is $90 + a$ eg</p> <ul style="list-style-type: none"> ■ $\angle ACB = 65$ (angles in a Z) ■ $\angle KCD = 35$ (angles in a Z) ■ $(65 + 35) - 90$ 	<p>! Angles identified through a single letter Condone if otherwise unambiguous eg, for identification of $\angle AKC$ accept</p> <ul style="list-style-type: none"> • K <p>✓ Minimally acceptable indication of method eg</p> <ul style="list-style-type: none"> •  •  •  •  •  <p>! Redundant angles identified The mathematical communication should not allow ambiguity. Hence for 3m all of the identified angles must be correct.</p> <p>Note to markers: The correct angles are:</p> 

Tier & Question									Angles again (cont)	
3-5	4-6	5-7	6-8							
	14	9	2			Correct response		Additional guidance		
				<i>or</i> 2m		<p>Indicates a is 10, even if the relevant angles are not identified clearly or correctly</p> <p>or</p> <p>Shows a complete correct method with the relevant angles clearly identified and with not more than one computational error; and follows through correctly to find their $\angle ACK$</p> <p>or</p> <p>Identifies clearly any two of the six correct angles as shown previously, even if others are incorrect</p>			<p>✓ <i>Minimally acceptable indication of method</i></p> <p>eg</p> <ul style="list-style-type: none">  	
				<i>or</i> 1m		<p>Shows a complete correct method with not more than one computational error; and follows through correctly to find their $\angle ACK$, but their angles are not clearly identified</p> <p>or</p> <p>Identifies clearly any one of the six correct angles as shown previously, even if others are incorrect</p>				

Tier & Question										Photos																										
3-5	4-6	5-7	6-8																																	
	15	10	3	Correct response				Additional guidance																												
				4m	<p>Gives a correct conclusion eg</p> <ul style="list-style-type: none"> ■ Film size 24, by £ 5.30 				<p>! Method used is price per photo This correct method will lead to a correct answer provided the values are not rounded or truncated If the values are rounded or truncated, mark as 1, 1, 0, 0 eg</p> <ul style="list-style-type: none"> • 24 size is 16p per photo, 36 is 17p per photo so 24 is cheaper by 1p per photo • $£3.74 \div 24 = 15\text{p}$, $£6.14 \div 36 = 17\text{p}$ 2×360 so £7.20 cheaper for 24 size 																											
				or	<p>Shows £ 56.1(0) and £ 61.4(0) (the correct total cost for both film sizes)</p> <p>or</p> <p>Concludes film size 24, by £ 8.30 (only error is to omit the cost of postage or assume the total postage is the same)</p> <p>or</p> <p>Shows £ 56.1(0) or £ 61.4(0), and at least two of the values shown in the table below for the other film size, then follows through to their final conclusion Note there must not be more than one error throughout</p> <table style="margin-left: 20px;"> <tr> <td style="border-right: 1px solid black; padding-right: 5px;">24 film</td> <td style="padding-left: 5px;">36 film</td> <td colspan="2"></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"><u>(56.10)</u></td> <td style="padding-left: 5px;"><u>(61.40)</u></td> <td colspan="2"></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;">£ 32.25</td> <td style="padding-left: 5px;">£ 26.5(0)</td> <td colspan="2">(buying film)</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;">£ 14.85</td> <td style="padding-left: 5px;">£ 28.9(0)</td> <td colspan="2">(printing film)</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;">£ 9</td> <td style="padding-left: 5px;">£ 6</td> <td colspan="2">(postage)</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;">£ 23.85</td> <td style="padding-left: 5px;">£ 34.9(0)</td> <td colspan="2">(printing & postage)</td> </tr> </table>								24 film	36 film			<u>(56.10)</u>	<u>(61.40)</u>			£ 32.25	£ 26.5(0)	(buying film)		£ 14.85	£ 28.9(0)	(printing film)		£ 9	£ 6	(postage)		£ 23.85	£ 34.9(0)	(printing & postage)	
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£ 9	£ 6	(postage)																																		
£ 23.85	£ 34.9(0)	(printing & postage)																																		
				2m									<p>Shows £ 56.1(0) or £ 61.4(0)</p> <p>or</p> <p>Shows all values correct from two rows of the table above</p> <p>or</p> <p>Shows £ 47.1(0) and £ 55.4(0) (error is to omit cost of postage)</p> <p>or</p> <p>Concludes film size 24, by £ 11.05 (only error is to omit cost of buying film)</p> <p>or</p> <p>Concludes film size 36, by £ 8.75 (only error is to omit cost of printing film)</p>																							
				or									<p>Shows all values correct from one row of the table above</p> <p>or</p> <p>Shows 15 and 10 (the correct number of films needed for both film sizes)</p>																							

Tier & Question							Equating	
3-5	4-6	5-7	6-8					
	16	11	4		Correct response	Additional guidance		
	a	a	a	1m	8	✓ <i>Values substituted into the given equations</i> Ignore ✗ <i>Incomplete processing</i>		
				1m	-3			
	b	b	b	1m	Writes a correct expression eg <ul style="list-style-type: none"> ■ $3a + 6b - (2c - d)$ ■ $3a + 6b - 2c + d$ ■ $3a + 6b - 3$ ■ $7(2c - d)$ ■ $14c - 7d$ ■ $2c - d + 18$ ■ $\frac{7}{8}(3a + 6b)$ 	✗ <i>Incorrect expression</i> eg <ul style="list-style-type: none"> ♦ $3a + 6b - 2c - d$ ♦ $7 \times 2c - d$ ♦ $2c - d \times 7$ ✗ <i>Expression uses only one of a or b, or only one of c or d</i> Note these are not possible without substitution of specific values and such expressions must therefore be incorrect		

Tier & Question							Correct response	Additional guidance
3-5	4-6	5-7	6-8	17				
a	a	a			1m	<p>Correct explanation that states the area of the rectangle is 6 and justifies why the area of the triangle is also 6</p> <p>The most common correct justifications for the triangle:</p> <p>Show, or imply by correct substitution, the relevant formula</p> <p>eg</p> <ul style="list-style-type: none"> ■ $\frac{1}{2} b \times h$ ■ $b \times h \div 2$ ■ $3 \times 4 \div 2$ ■ 1.5×4 <p>Divide the triangle into two parts as shown, then justify why the area of the smaller triangle is 1.5</p> <p>eg</p> <ul style="list-style-type: none"> ■  Area of A = 4.5 Area of rest of shape would be 2 but half is not shaded, so it's $4.5 + 2 - 0.5$ <p>Show the area of the triangle is half that of the enclosing square, less 2</p> <p>eg</p> <ul style="list-style-type: none"> ■  Area = $4^2 \div 2 - 2$ <p>Show correct groupings</p> <p>eg</p> <ul style="list-style-type: none"> ■  Area of triangle is 5 as shown and the bits shaded black makes 6 <p>Use dissection</p> <p>eg</p> <ul style="list-style-type: none"> ■  	<p>Same areas</p> <p>! Units given Ignore</p> <p>! Areas not evaluated Accept if unambiguous and equated eg</p> <ul style="list-style-type: none"> • $3 \times 2 = 3 \times 4 \div 2$ <p>✗ Incomplete explanation eg</p> <ul style="list-style-type: none"> • You add up the halves • Count the squares, join halves then join little bits to make 6 <p>✗ Spurious explanation eg</p> <ul style="list-style-type: none"> • One of the sloping sides marked as 4 and used as the height of the triangle • Triangle incorrectly grouped to show 6 <p>Note to markers: Correct responses based on grouping must include the following pairings:</p> 	

Tier & Question									Same areas (cont)		
3-5	4-6	5-7	6-8								
							Correct response		Additional guidance		
	17	12	5								
	b	b	b	1m	<p>Draws a parallelogram, with no right angles, that has an area of 6 eg, base 3 perpendicular height 2, or vice-versa</p> <ul style="list-style-type: none"> ▪  <p>eg, base 6 perpendicular height 1, or vice-versa</p> <ul style="list-style-type: none"> ▪  <p>eg, a parallelogram consisting of two triangles each of base 3 and height 2, or vice-versa</p> <ul style="list-style-type: none"> ▪  						<p>! <i>Not accurate and/or lines not ruled</i> Accept provided the pupil's intention is clear</p>

Tier & Question						Libraries	
3-5	4-6	5-7	6-8				
18	13	6			Correct response	Additional guidance	
a	a	a	1m	Indicates 'False' and gives a correct justification	<p>! <i>Values read from the graph or calculated</i> Accept 725 ± 10 and 362.5 ± 10 and qualified approximations such as 'about 700' but do not accept incorrect calculations eg</p> <ul style="list-style-type: none"> • $725 \div 2 = 312.5$ (error) < 500 <p>✓ <i>Minimally acceptable justification</i> eg</p> <ul style="list-style-type: none"> • Half of 725 is 362.5 not 500 • The graph doesn't fall as low as 360 <p>✗ <i>The significance of 362.5 (± 10) is not interpreted</i> eg</p> <ul style="list-style-type: none"> • Half of 725 is 362.5 <p>✓ <i>Minimally acceptable justification</i> eg</p> <ul style="list-style-type: none"> • It only dropped from 725 to 500 • 725 halved isn't 500 • 500 is not half of 725 <p>✗ <i>Numbers stated without interpretation</i> eg</p> <ul style="list-style-type: none"> • It dropped from 725 to 500 <p>! <i>Ambiguous reference to 'more than half' or 'less than half'</i> As the reference could be to the fall or the number of libraries open, condone</p> <p>✓ <i>Explanation interprets the misconception prompted by the graph</i> eg</p> <ul style="list-style-type: none"> • Because the scale doesn't start at zero, it looks as if it has dropped much more than it has in reality 		
				The most common correct justifications:			
				Interpret the significance of 362.5 (± 10) eg			
				<ul style="list-style-type: none"> ■ Half of 725 is 362.5 but it only fell to 500 ■ $363 < 500$ ■ It fell to 500 but it should have dropped to about 360 ■ The drop is about 225 but it would need to be 362.5 			
				State or imply that half of $725 < 500$ eg			
				<ul style="list-style-type: none"> ■ 500 is more than half of 725 			
				State or imply that $500 \times 2 > 725$ eg			
				<ul style="list-style-type: none"> ■ If you double the value for 1998 you would get 1000 libraries but there were far fewer than that open in 1988 			

Tier & Question								Libraries (cont)	
3-5	4-6	5-7	6-8						
	18	13	6			Correct response		Additional guidance	
	b	b	b	1m		<p>Indicates 'Cannot be certain' and gives a correct justification that you cannot predict beyond the data set</p> <p>eg</p> <ul style="list-style-type: none"> ■ No data is given for those years ■ The diagram doesn't show 2004 so there is not enough information ■ The trend might change ■ Although the graph shows the number is decreasing, we cannot know for certain that it will continue 		<p>✓ <i>Minimally acceptable justification</i></p> <p>eg</p> <ul style="list-style-type: none"> • The diagram doesn't show 2004 • It only goes to 1998 • You can't predict the future • Who can tell what will happen? • Anything might happen • They might decide they've closed enough • There could be an increase or a decrease • More libraries could open • There is not enough information given <p>! <i>Justification describes the graph</i></p> <p>Ignore if accompanying a correct response, otherwise do not accept</p> <p>eg, accept</p> <ul style="list-style-type: none"> • The graph is not falling at a steady rate and anything might happen <p>eg, do not accept</p> <ul style="list-style-type: none"> • It is not falling at a steady rate • The chart doesn't go in a steady pattern • It is levelling out so there will probably be about 475 <p>✗ <i>Incomplete justification</i></p> <p>eg</p> <ul style="list-style-type: none"> • Some libraries could close down • It is uncertain 	

Tier & Question					Marking overlay available		Equations	
3-5	4-6	5-7	6-8					
	19	14	7			Correct response	Additional guidance	
		a	a	1m	Draws a straight line within the tolerance, and at least of length, as specified by the overlay	<p>! <i>Points not plotted</i> Ignore</p> <p>× <i>Points not joined</i></p>		
		b	b	2m	Draws a curve within the tolerance as specified by the overlay between (1, 12) and (12, 1), even if the curve is incorrect or omitted elsewhere			
				or 1m	The curve is within tolerance between (2, 6) and (6, 2), even if incorrect or omitted elsewhere			
					or			
					Plots 6 points correctly			

Tier & Question					Walk	
3-5	4-6	5-7	6-8			
	20	15	8		Correct response	Additional guidance
				1m	Indicates 'steady speed', ie	
					<input type="checkbox"/>	
					<input type="checkbox"/>	
					<input type="checkbox"/>	
					<input checked="" type="checkbox"/>	
					<input type="checkbox"/>	

Tier & Question									Swimming clubs	
3-5	4-6	5-7	6-8							
		16	9							
		a	a	1m	Both correct, ie Mean as 25 years 3 months Range as 4 years 8 months					✓ <i>Years and months omitted</i> eg • 25, 3 4, 8
		b	b	1m	Indicates 'less than 1 year', ie <input type="checkbox"/> <input type="checkbox"/> <input checked="" type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>					
				1m	Indicates 'not possible to tell', ie <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input checked="" type="checkbox"/>					

Tier & Question					<i>Marking overlay available</i>		Arrow
3-5	4-6	5-7	6-8				
		21	17	10	Correct response		Additional guidance
		a	a	2m	Correct enlargement within the tolerance as shown on the overlay, with vertices joined	! <i>Lines not ruled</i> Accept provided the pupil's intention is clear ! <i>Construction lines shown</i> Ignore ✓ <i>For 1m, scale factor – 2</i>	
				or 1m	At least 5 vertices correct		
				or 1m	The only error is to use an incorrect centre of enlargement, ie the enlargement is the correct size as shown by the overlay, with vertices joined, but is in the incorrect place		
		b	b	1m	Arrow head length as 4		
				1m	Angle as 40		
				1m	Vertical height as 12		

Tier & Question							Questions
3-5	4-6	5-7	6-8				
		18	11	Correct response		Additional guidance	
		a	a	1m	0.15 or equivalent probability		
				1m	0.65 or equivalent probability		
		b	b	1m	14	✓ <i>40 used within the answer</i> Accept eg <ul style="list-style-type: none"> • 14 out of 40 • $\frac{14}{40}$ 	

Circling

Tier & Question					Correct response	Additional guidance						
3-5	4-6	5-7	6-8									
		19	12									
				3m	25π or 78.5(...) or 79	<p>✗ For 3m, percentage truncated to 78</p> <p>! <i>Incorrect units seen within working</i> Ignore</p> <p>The following values are commonly seen Markers may find them useful</p> <table style="margin-left: 40px;"> <tr> <td>$\pi \times 3^2$</td> <td>28, 28.2(...), 28.3</td> </tr> <tr> <td>$(\pi \times 3)^2$</td> <td>88 to 89 inclusive</td> </tr> <tr> <td>$\pi^2 \times 3$</td> <td>29 to 30 inclusive</td> </tr> </table> <p>! $\pi 3^2$ <i>not evaluated or otherwise interpreted</i> As a common error is to evaluate $\pi 3^2$ as $(\pi 3)^2$, do not accept as evidence of a correct method</p>	$\pi \times 3^2$	28, 28.2(...), 28.3	$(\pi \times 3)^2$	88 to 89 inclusive	$\pi^2 \times 3$	29 to 30 inclusive
$\pi \times 3^2$	28, 28.2(...), 28.3											
$(\pi \times 3)^2$	88 to 89 inclusive											
$\pi^2 \times 3$	29 to 30 inclusive											
				or 2m	Shows or implies a correct method, even if values have been rounded or truncated eg <ul style="list-style-type: none"> ■ $\frac{9\pi}{36} \times 100$ ■ $9\pi \div 36$ ■ $\frac{\pi}{4}$ ■ $28.2(\dots) \div 6^2$ ■ $9\pi = 28$ (<i>rounded</i>), $28 \div 36 = 0.778$ ■ $36 - 28.2$ (<i>truncated</i>) = 7.8, $7.8 \div 36 = 22$ (<i>rounded</i>), $100 - 22$ ■ 78 <p>or</p> <p>The only error is to give the percentage that is not shaded, ie 21.5 or 21.4(...) or 21</p>							
				or 1m	Shows or implies a correct method for the area of the circle, even if the value has been rounded or truncated eg <ul style="list-style-type: none"> ■ 9π ■ $3 \times 3 \times \pi$ ■ 28.27(...) ■ 28 <p>or</p> <p>Divides their area, even if incorrect, by 36 eg <ul style="list-style-type: none"> ■ $\pi 3^2 = 88.8$, $88.8 \div 36$ </p>	<p>✓ <i>Their area represents the unshaded part of the diagram</i></p>						

Tier & Question					13	Correct response	Additional guidance									
3-5	4-6	5-7	6-8													
				b	3m	<p>Gives a value that is greater than 132 but smaller than or equal to 133, and shows a complete correct method that encompasses the stages described below</p> <ol style="list-style-type: none"> The correct mid-points of 128, 133 and 138 are identified The percentages used are within range and sum to 100 The intention to multiply mid-points by percentages is shown or implied The answer is calculated correctly from the sum of their multiplications 	<p>! Range of percentages Accept within the following values: 21 to 24 inclusive, 59 to 62 inclusive, 16 to 19 inclusive</p> <p>! Stage 3 not shown and their mean is given to the nearest integer As spurious methods lead to seemingly correct values, do not accept as evidence of the intention to multiply</p>									
					or 2m	<p>Within an otherwise correct method, only one of stages 1, 2 and 4 is incorrect, or stage 4 is omitted</p> <p>eg, stage 1 incorrect</p> <ul style="list-style-type: none"> $21 \times 128.5 + 60 \times 133.5 + 19 \times 138.5 = 13340$ so mean is 133.4 <p>eg, stage 2 incorrect</p> <ul style="list-style-type: none"> <table style="border: none;"> <tr> <td style="padding-right: 20px;">128</td> <td style="padding-right: 20px;">22</td> <td>2816</td> </tr> <tr> <td>133</td> <td>62</td> <td>8246</td> </tr> <tr> <td>138</td> <td>18</td> <td>2484 (<i>% sum to 102</i>)</td> </tr> </table> $13546 \div 100$ (or 102), mean is 135 (or 133) <p>eg, stage 4 omitted</p> <ul style="list-style-type: none"> $128 \times 22 = 2816$ $133 \times 61 = 8113$ $138 \times 17 = 2346$ 	128	22	2816	133	62	8246	138	18	2484 (<i>% sum to 102</i>)	
128	22	2816														
133	62	8246														
138	18	2484 (<i>% sum to 102</i>)														
					or 1m	<p>Within an otherwise correct method, two of the stages are incorrect</p> <p>eg, stages 1 and 2 incorrect</p> <ul style="list-style-type: none"> <table style="border: none;"> <tr> <td style="padding-right: 20px;">128.5</td> <td>20</td> </tr> <tr> <td>133</td> <td>60</td> </tr> <tr> <td>138.5</td> <td>20</td> </tr> </table> $13320 \div 100 = 133.2$ (stage 3 not shown but implied both by the correct total and the corresponding mean) 	128.5	20	133	60	138.5	20				
128.5	20															
133	60															
138.5	20															

Tier & Question										Percentage change	
3-5	4-6	5-7	6-8								
		21	14								
		a	a	1m	Indicates 70×1.09						
				1m	<p>Gives a correct numerical interpretation for one of the calculations, even if it is not in question form</p> <p>eg, for 70×0.9</p> <ul style="list-style-type: none"> ■ What is 70 decreased by 10%? ■ Find 90% of 70 ■ What is 70% of 90? ■ What is $\frac{9}{10}$ of 70? <p>eg, for 70×1.9</p> <ul style="list-style-type: none"> ■ It increases 70 by 90% ■ 190% of 70 <p>eg, for 70×0.09</p> <ul style="list-style-type: none"> ■ What is 9% of 70? ■ 70 decreased by 91% 				<p>! <i>Units or context given</i> Ignore</p> <p>! <i>Two or more steps used</i> eg, for 70×1.9</p> <ul style="list-style-type: none"> ♦ Finds 90% of 70 then adds it on to 70 <p>Penalise only the first occurrence</p> <p>! <i>Multiplication sign not interpreted</i> eg, for 70×1.9</p> <ul style="list-style-type: none"> ♦ $70 \times 190\%$ <p>Penalise only the first occurrence</p> <p>× <i>Incorrect response</i> eg, for 70×1.9</p> <ul style="list-style-type: none"> ♦ Increase 70 by 190% 		
				1m	Gives a correct interpretation for a different calculation						× 70×1.09 not chosen for the first mark, but interpreted later
		b	b	1m	0.86						<p>× <i>Two-step process</i></p> <p>× <i>Incorrect % sign</i> eg</p> <ul style="list-style-type: none"> ♦ 0.86%
		c		2m	21						
				or 1m	<p>Shows the value 121</p> <p>or</p> <p>Shows a correct method, working only with the percentage increases</p> <p>eg</p> <ul style="list-style-type: none"> ■ 1.1^2 ■ 110×1.1 ■ $110 + 11$ <p>or</p> <p>Shows a complete correct method with not more than one computational error</p> <p>eg</p> <ul style="list-style-type: none"> ■ $70 + 10\% = 77$ $77 + 10\% = 84.7$ $\left(\frac{84.7 - 70}{70}\right) \times 100$ ■ 10 increased by 10% is 11 11 increased by 10% is 12.1 2.1×10 						

Tier & Question					15	Correct response	Additional guidance	Star
3-5	4-6	5-7	6-8					
			a	1m	<p>Correct interpretation</p> <p>eg</p> <ul style="list-style-type: none"> ■ Number of hours it would take the spaceship to travel from Earth to the star ■ How many hours the journey would take 	<p>✓ <i>Minimally acceptable explanation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Number of hours to travel ♦ How many hours it takes ♦ Time taken to travel at 40 000 km per hour <p>✗ <i>Incomplete interpretation that does not refer to both the journey and the units of time</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Number of hours ♦ How long it takes ♦ Time taken to travel <p>✗ <i>No interpretation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Distance times light-years divided by speed 		
				1m	<p>Correct interpretation</p> <p>eg</p> <ul style="list-style-type: none"> ■ Number of years it would take the spaceship to travel from Earth to the nearest star ■ Number of years from E to PC 	<p>✓ <i>Minimally acceptable explanation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Number of years to travel ♦ How many years to get there <p>✓ <i>Incomplete interpretation that does not refer to the journey</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Number of years <p>✗ <i>Incomplete interpretation that does not refer to the units of time</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Time taken to travel <p>✗ <i>Incorrect interpretation</i></p> <p>eg</p> <ul style="list-style-type: none"> ♦ Time taken to travel in years and in days 		
			b	1m	114 000			

Tier & Question					16		Correct response		Additional guidance	
3-5	4-6	5-7	6-8							
				a	2m	8.4(...)			<p>! Answer 8 Accept provided a correct method or a more accurate value is seen</p>	
					or 1m	Shows a correct method eg <ul style="list-style-type: none"> ■ $14 \times \sin 37$ or Shows a correct trigonometric ratio eg <ul style="list-style-type: none"> ■ $\sin 37 = \frac{y}{14}$ 			<p>✓ Change of variable</p> <p>! Incomplete notation that omits the angle eg <ul style="list-style-type: none"> ♦ $\sin = \frac{y}{14}$ Do not accept unless evaluation or other indication shows that the relevance of the angle has been understood</p>	
				b	2m	64.6(...)			<p>! Answer 65 Accept provided a correct method or a more accurate value is seen</p>	
					or 1m	Uses 6 and 14 to form a correct trigonometric ratio using cosine, even if rounded or truncated eg <ul style="list-style-type: none"> ■ $\cos^{-1} \frac{6}{14}$ ■ $\cos m = \frac{6}{14}$ ■ $\cos m = 0.42857...$ ■ $\cos m = 0.43$ or Gives the answer 64 or 64.5(...) or Shows a complete correct method eg <ul style="list-style-type: none"> ■ $90 - \sin^{-1} \frac{6}{14}$ 			<p>✓ Change of variable</p> <p>✓ Incomplete but unambiguous notation eg <ul style="list-style-type: none"> ♦ $\cos = \frac{6}{14}$ </p>	

Satellite

Tier & Question					17	Correct response	Additional guidance
3-5	4-6	5-7	6-8				
					<p>3m</p> <p>27143.(...) or 8640π</p> <p>or</p> <p>2m</p> <p>Shows a complete correct method even if values are rounded or truncated</p> <p>eg</p> <ul style="list-style-type: none"> ■ $C = 2\pi r = 14400\pi$, so speed is $14400\pi \div 100 \times 60$ ■ $(12800 + 1600) \times \pi \times \frac{3}{5}$ ■ $(14400 \times 3.14) \times 60 \div 100$ <p>or</p> <p>Shows a correct value in km/min</p> <p>eg</p> <ul style="list-style-type: none"> ■ 144π ■ 452.(...) <p>or</p> <p>The only error is to omit to add one of the values of 800</p> <p>eg</p> <ul style="list-style-type: none"> ■ 8160π ■ 25635.(...) <p>or</p> <p>1m</p> <p>Shows or implies the correct length of one orbit</p> <p>eg</p> <ul style="list-style-type: none"> ■ 14400π ■ $7200 \times 2\pi$ ■ $(12800 + 2 \times 800) \times \pi$ ■ 45238.9(...) <p>or</p> <p>Shows or implies both $\div 100$ and $\times 60$</p> <p>eg</p> <ul style="list-style-type: none"> ■ $\times \frac{3}{5}$ ■ $\times 0.6$ ■ $\div 1.666666(...)$ ■ $\div (100 \div 60)$ ■ 7680π (no values of 800 added) ■ 24127.(...) (no values of 800 added) ■ 8640 (π omitted throughout) 	<p>! <i>Answer rounded to 30000</i></p> <p>Accept provided a correct method or a more accurate value is seen</p> <p>! <i>Answer 27000 or 27100 or 27140</i></p> <p>Accept provided no incorrect method is seen</p> <p> </p> <p>✓ <i>For this mark, $\div 100 \times 60$ converted to a decimal which is rounded or truncated</i></p> <p>eg</p> <ul style="list-style-type: none"> ◆ 1.7 ◆ 1.66 	

Tier & Question					18	Correct response	Additional guidance
3-5	4-6	5-7	6-8				
			a	1m	Correct explanation eg ■ $\frac{a^2 - b^2}{a - b} = \frac{(a - b)(a + b)}{a - b}$	✓ Minimally acceptable explanation eg ♦ $a^2 - b^2 = (a - b)(a + b)$! Numerical substitution Ignore if accompanying a correct algebraic explanation, otherwise do not accept	
			b	1m	a	✓ a^1 or $a^1 b^0$	
			c	2m or 1m	$a - b$ Shows a correct partial simplification eg ■ $\frac{a^2b - ab^2}{ab}$ (dividing through by ab) ■ $\frac{a^3 - a^2b}{a^2}$ (dividing through by b^2) ■ $a - \frac{a^2b^3}{a^2b^2}$ (partial fractions, first term simplified)	✗ Incorrect simplification eg ♦ $\frac{a - a^2b^3}{a^2b^2}$	

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